

Système de points matériels: aide-mémoire

Définitions générales	$M = \sum_{\alpha} m_{\alpha} \quad \vec{p} = \sum_{\alpha} \vec{p}_{\alpha} \quad \vec{F}^{\text{ext}} = \sum_{\alpha} \vec{F}_{\alpha}^{\text{ext}}$			
Référentiel	Labo			Centre de masse
Point	O fixe	A = A(t) quelconque	G = Centre de masse	G = Centre de masse
Définitions, relations, propriétés	$\vec{OP}_{\alpha} = \vec{r}_{\alpha} \quad \frac{d\vec{OP}_{\alpha}}{dt} = \vec{v}_{\alpha}$	$\vec{OP}_{\alpha} = \vec{OA} + \vec{AP}_{\alpha}$	$\vec{OP}_{\alpha} = \vec{OG} + \vec{GP}_{\alpha}$ $\vec{OG} = \frac{1}{M} \sum_{\alpha} m_{\alpha} \vec{r}_{\alpha}$ $\vec{v}_G = \frac{1}{M} \sum_{\alpha} m_{\alpha} \vec{v}_{\alpha}$	$\vec{GP}_{\alpha} = \vec{r}_{\alpha}^* \quad \frac{d\vec{GP}_{\alpha}}{dt} = \vec{v}_{\alpha}^*$ $\vec{v}_{\alpha} = \vec{v}_G + \vec{v}_{\alpha}^*$ $\sum_{\alpha} m_{\alpha} \vec{r}_{\alpha}^* = 0 \quad \vec{p}^* = 0$
Moment des forces	$\vec{M}_O = \vec{M}_O^{\text{ext}} = \sum_{\alpha} \vec{OP}_{\alpha} \times \vec{F}_{\alpha}^{\text{ext}}$	$\vec{M}_A = \vec{M}_A^{\text{ext}} = \sum_{\alpha} \vec{AP}_{\alpha} \times \vec{F}_{\alpha}^{\text{ext}}$	$\vec{M}_G = \vec{M}_G^{\text{ext}} = \sum_{\alpha} \vec{GP}_{\alpha} \times \vec{F}_{\alpha}^{\text{ext}}$	$\vec{M}_G^{\text{ext}*} = \sum_{\alpha} \vec{GP}_{\alpha} \times \vec{F}_{\alpha}^{\text{ext}} = \vec{M}_G^{\text{ext}}$
Moment cinétique	$\vec{L}_O = \sum_{\alpha} \vec{OP}_{\alpha} \times m_{\alpha} \vec{v}_{\alpha}$	$\vec{L}_A = \sum_{\alpha} \vec{AP}_{\alpha} \times m_{\alpha} \vec{v}_{\alpha}$	$\vec{L}_G = \sum_{\alpha} \vec{GP}_{\alpha} \times m_{\alpha} \vec{v}_{\alpha}$	$\vec{L}_G^* = \sum_{\alpha} \vec{GP}_{\alpha} \times m_{\alpha} \vec{v}_{\alpha}^*$
Théorème du transfert		$\vec{L}_A = \vec{L}_O - \vec{OA} \wedge M \vec{v}_G$	$\vec{L}_G = \vec{L}_O - \vec{OG} \wedge M \vec{v}_G$	
Théorème de Koenig 1				$\vec{L}_A = \vec{AG} \wedge M \vec{v}_G + \vec{L}_G^*$ $\vec{L}_G = \vec{L}_G^*$
Théorème du moment cinétique	$\frac{d\vec{L}_O}{dt} = \vec{M}_O^{\text{ext}}$	$\frac{d\vec{L}_A}{dt} = -\vec{v}_A \wedge M \vec{v}_G + \vec{M}_A^{\text{ext}}$	$\frac{d\vec{L}_G}{dt} = \vec{M}_G^{\text{ext}}$	$\frac{d\vec{L}_G^*}{dt} = \vec{M}_G^{\text{ext}*}$
Loi de Newton	$M \vec{v}_G = \vec{p} \quad M \vec{a}_G = \vec{F}^{\text{ext}} \quad \frac{d\vec{p}}{dt} = \vec{F}^{\text{ext}}$			$\frac{d\vec{p}^*}{dt} = 0$
Energie cinétique	$E_{\text{cin}} = \sum_{\alpha} \frac{1}{2} m_{\alpha} v_{\alpha}^2$			$E_{\text{cin}}^* = \sum_{\alpha} \frac{1}{2} m_{\alpha} v_{\alpha}^{*2}$
Théorème de Koenig 2				$E_{\text{cin}} = \frac{1}{2} M v_G^2 + E_{\text{cin}}^*$